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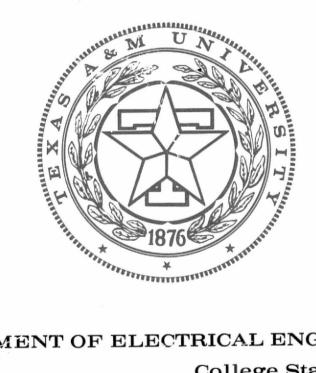
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TEXAS A&M UNIVERSITY

THE DESIGN, ANALYSIS AND EXPERIMENTAL EVALUATION OF AN ELASTIC MODEL WING

by

Ralph K. Cavin, III and Chavalit Thisayakorn





DEPARTMENT OF ELECTRICAL ENGINEERING College Station, Texas

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Texas A&M University

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(I) Introduction

It is common practice in preliminary static aeroelastic analyses to estimate clastic increments in stability derivatives by utilizing a clamped-vehicle stiffness matrix in conjunction with an aerodynamic influence matrix determined for the configuration by use of the linear, inviscid aerodynamic theory. These aeroelastic estimates are normally refined by 'freeing' the structure and including vehicle mass effects based upon the use of mean axis vehicle coordinate systems. [1] The computer program FLEXSTAB, which was written by The Boeing Airplane Company under the sponsorship of NASA-AMES, is a relatively sophisticated implementation of these basic ideas. FLEXSTAB has the capability of admitting two different types of structural representations. If the structural characteristics of the vehicle are adequately represented by the interconnection of beam elements, then FLEXSTAB accepts the beam EI and GK characteristics and generates the required structural matrices. On the other hand, the structural matrices can be generated externally in a finite element program, without the restriction of beam-like structural properties, and the results can be entered directly into FLEXSTAB.

The primary objective of this study was to develop experimental data from a carefully controlled elastic model to be used in evaluating the effectiveness of aeroelasticity programs such as FLEXSTAB for vehicles of the orbiter class. In order to accomplish this objective at a minimum cost it was decided to utilize an existing rigid 5% fuselage model for the OO2 Orbiter configuration,

and to construct elastic wings for the model. The 002 Orbiter wings were straight with moderate aspect ratio and were therefore amenable to a beam-like structural representation.

(II) Design and Fabrication of the Elastic Wing

In view of the assumed beam-like structure of the 002 Orbiter wing, it was decided that the load carrying member of the model wing should be a beam with well defined EI and GK characteristics. It was further decided that the distribution of EI and GK along the wing span should parallel the 002 EI and GK shapes provided to A&M by the NASA-JSC Structures group. However, no attempt was made to scale the given (Stiff) beam characteristics to the 5% model. Rather the selection of EI and GK was based upon the criterion that measurable deformations and stability derivative changes should occur under expected aerodynamic load.

The basic design philosophy that evolved was that the aerodynamic loads should be transmitted to the beam via rib members. Further, in order to approximate the finite-element aerodynamic methods, the wing surface was segmented in a streamwise manner and each segment was rigidly attached to a corresponding rib element. Figure 1 is a planform view showing location of the Elastic Axis, as well as the basic aerodynamic sections for the wing. The NACA airfoil descriptions are given in Figure 2. As can be seen from Figure 1, the elastic axis is swept aft at an angle of 9.75 degrees from the vertical.

Figure 3 depicts the basic construction of the elastic wing. Note that each panel section is made of low density Balsa Wood which is cemented to the supporting rib member. The region between adjacent panel sections is approximately 1/16" wide and is filled with an ultra soft Neoprene gasket that

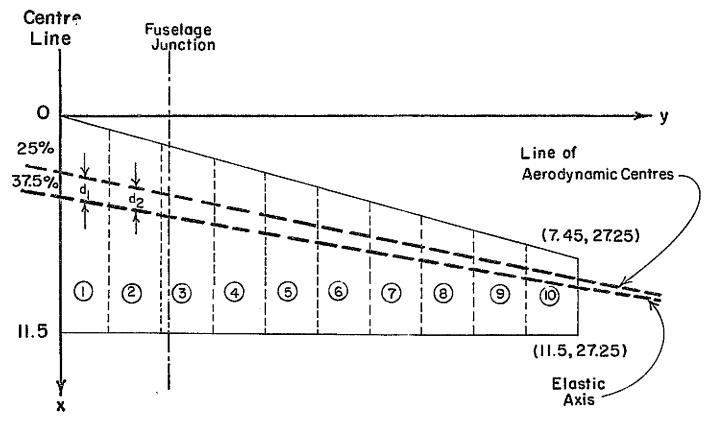


FIGURE 1. Elastic Model Wing Planform (5% 002 orbiter wing)

AIR-FOIL: ROOT NACA OOI4
TIP NACA OOIO

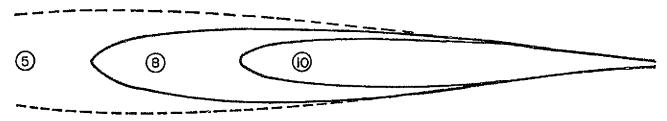
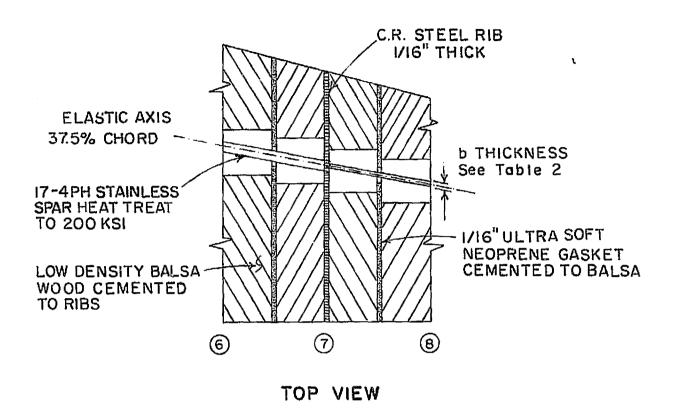


FIGURE 2. Rib - Airfoil (full size model wing cross-sections)



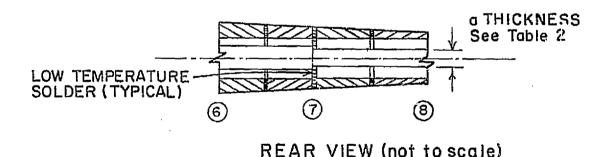


FIGURE 3. Cross-Sectional structural description at the Model-Wing Construction.

is cemented to the Balsa. Stress Calculations indicated that a high strength alloy of stainless steel could be used for the wing spar but that heat treatment was required after machining. This process allowed a 2.5 safety factor on ultimate strength and about 2.3 on yield strength. (No allowance was made for dynamic loads.) Ribs were made of the same material as the spar for ease of attachment. The spar was designed to have a rectangular cross section so that the rib elements could be firmly attached to the spar. Table 1 contains the dimensional data for the spar. The computed values for EI and GK are also listed in this table. The cross sectional moment data which was computed by using the formulae [4]

$$K = \frac{ba^{3}}{3} - \frac{64a^{4}}{\pi^{5}} \tanh(\frac{\pi b}{2a}) . \tag{1}$$

$$I_x = \int z^2 dA = \frac{ba^3}{12}$$
 (2)

The above symbols are defined in Figure 4.

(III) Design Calculations

The purpose of this section is to describe the analysis methods that were utilized in the design of the elastic wing described in Section II. Two basic analytical tools were utilized in the evolution of structural specifications for the wing; namely the Doublet Lattice Aerodynamic lifting surface procedure and the finite element structural analysis method for beam members. In the following, we first discuss the analytical formulation for the general, time-dependent problem. After this broad notational framework has been established, the special static-aeroelastic and flutter problems are considered.

A. The Structural Model

As has already been pointed out, the principal load-carrying member in the wing structure is the spar element. The spar is essentially a beam element with

Spanwise Panel (location number)	b - Thickness (inches)	a - Thickness (inches)	Lengths (inches)
2–3	0.391	0.407	1.078
3–4	0.369	0.355	2.828
4-5	0.273	0.368	2,828
5–6	0.243	0.310	2.828
: 6–7	0.173	0.300	2.828
7-8	0.152	0.246	2.828
8–9	0.1/16	0.188	2.828
910	0.129	0.152	2.891

Table 1. Spar Dimensions (See also Figure 3)

Station Number of Spanwise Segments	Values of EI (1.b - in ²)	Values of GK (1b - in ²)
3	63687.50	40090.40
<u> </u>	39837.50	27166.72
5	32875.00	15314.09
6	17575.00	8730.85
7	11325.00	3718.85
8	5468.75	1990.35
9	2343.75	1156.62
10	1093.75	600.77

Table 1. (continued)

Values of EI and GK for wing spar

$$E = 2.9 \times 10^{7}$$
 lb/in^{2}
 $G = 1.12 \times 10^{7}$ lb/in^{2}

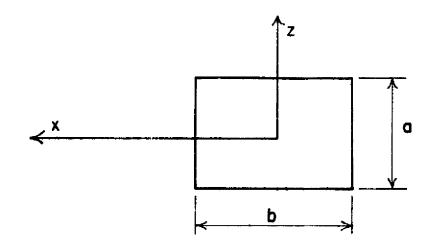


FIGURE 4. Definition of symbols for beam Cross - section.

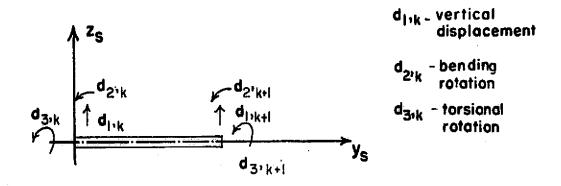
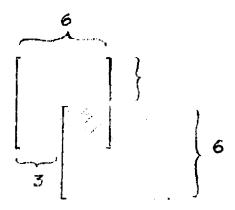


FIGURE 5. Definition of structural nodal displacements.

rectangular sections of length 2.8 in. whose sectional area progressively decreases in the spanwise direction. There are 8 spar sections, each with a possibility of 6 physical degrees of freedom per section, implying a maximum of 40 structural degrees of freedom. However, in view of the planned testing of the wing at very small (less than ten degrees) angles of attack, it was decided that in-plane bending of the spar would be minimal and hence only torsional and normal bending degrees of freedom were retained for each beam element. The degrees of freedom associated with each element are defined in Figure 5. The elemental stiffness matrix for the member shown in Figure 5 therefore reduces to [2].

A composite stiffness matrix can be generated by appropriately combining the element matrices in an underlying structural reference frame. In view of the fact that the spar is straight, the assembly task is quite straight-forward in this case and can be accomplished by overlaying successive element matrices and adding overlapping terms, e.g.,



Of course the left end of the inboard spar element is constrained to have no degrees of freedom since the flexible wing is attached to the fuselage at this point.

A generalized mass matrix can be formulated for the flexible wing by using the results given in [2], i.e., the mass matrix for the element in Figure 5 is

$$[M]_{K} = \begin{bmatrix} \frac{13}{35} + \frac{6I_{x}}{x} \\ \frac{11\ell}{210} + \frac{I_{x}}{10A\ell} & \frac{\ell^{2}}{105} & \frac{2I_{x}}{15A} & \text{symmetric} \\ 0 & 0 & \frac{J_{y}}{3A} \\ \frac{9}{70} - \frac{6I_{x}}{5A\ell^{2}} & \frac{13\ell}{420} - \frac{I_{x}}{10AC} & 0 & \frac{13}{35} + \frac{6I_{x}}{5AC^{2}} \\ -\frac{13\ell}{420} + \frac{I_{x}}{10A\ell} & \frac{-\ell^{2}}{140} - \frac{I_{x}}{30A} & 0 & \frac{-11\ell}{210} - \frac{I_{x}}{10A\ell} & \frac{\ell^{2}}{105} + \frac{2I_{x}}{15A} \\ 0 & 0 & \frac{J_{y}}{6A} & 0 & 0 & \frac{J_{y}}{3A} \end{bmatrix}$$

$$(4)$$

As in the case of the stiffness matrix, assembly of a composite mass matrix for the wing can be accomplished by appropriately combining the matrices, $[M]_K$, K = 1, ..., 8. The effects of rib mass were included by simply adding lumped mass and inertia terms to the diagonal elements of the spar mass matrix. A summary of rib mass properties is given in Table 2.

Station number of ribs	Distances of ribs' c.g. off from the elastic axis (in.)	Rib mass (slug) x 10 ⁻³	Polar Mass moment of inertia (slug-in ²) x 10 ⁻²
3	0.706527	0.243999	0.140291
\mathfrak{f}_{μ}	0.651691	0.201206	0.098401
5	0.596856	0.163412	0.067019
6	0.542019	0.130345	0.044076
7	0.487183	0.101735	0.027786
8	0.432345	0.077311	0.016626
9	0.377509	0.0568	0.009311
10	0.322672	0.039931	0.004781

Table 2. Data on steel ribs of the wing

Since the wing spar is swept at an angle. A, of 9.75 degrees, it is necessary to transform the spar structural matrices into a coordinate frame compatible with the acrody, and frame. This is easily accomplished by performing the following transformation

$$[K]_1 = [T] [K] [T]^T$$

where
$$T = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & \cos \theta & -\sin \theta & 0 & 0 & 0 & 0 \\ 0 & \sin \theta & \cos \theta & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & \cos \theta & -\sin \theta \\ 0 & 0 & 0 & 0 & \sin \theta & \cos \theta \end{bmatrix}$$

B. Aerodynamics Development

The basic procedure that has been used to treat aerodynamic forces is based on the Doublet-Lattice-Method (D.L.M.) [3]. Fundamentally, the D.L.M. yields a set of <u>Aerodynamic Influence Coefficients</u>, [D], relating the assumed harmonic motion of the normal wash, {w}, at specified points on the wing surface to the <u>pressure</u> differential, {ACp}, across the wing. Specifically, the integral equation

$$\mathbf{w}(\mathbf{x},\mathbf{y},\mathbf{z}) = \frac{1}{8\pi} \int \mathbf{K}(\mathbf{x}-\boldsymbol{\xi}, \mathbf{y}-\mathbf{n}, \mathbf{z}-\boldsymbol{\zeta}; \boldsymbol{\omega}, \mathbf{M}) \Delta \mathbf{C} \mathbf{p} \, d\boldsymbol{\xi} \, d\boldsymbol{\sigma}$$
 (5)

is approximately solved as

$$\{\mathbf{w}\} = [\mathbf{D}] \{\Delta \mathbf{C}\mathbf{p}\} \tag{6}$$

where the velocity normal to the oscillating surface is

$$\{W\} = U_{\infty} \operatorname{Re} \left[\{w\} e^{i\omega t} \right], \tag{7}$$

and the pressure differential is

$$\{\Delta p\} = q_{\infty} \operatorname{Re} \left[\{\Delta C p\} e^{i\omega t} \right].$$
 (8)

Let us now consider specifically the computation of the aerodynamic forces for later use.

In general, l_{ij} is the distance from the jth. structural node to the 1/4 chord point for the ijth, panel and r_{ij} is the distance from the jth, structural node to the 3/4 chord point for the ijth, panel (See Figure 6). The total force acting on the ijth, panel is given by

$$f_{i,j} = \Delta p_{i,j} A_{i,j} \tag{9}$$

and will be assumed to be acting at the center of the 3/4 chord point of the ijth. panel. In order to define the sense of the various forces and moments due to the aerodynamic forces, we must first define the assumed positive displacement at node j. This is done in Figure 7, the force tending to increase the dl coordinate is

$$f_{i,j} = \sum_{i=1}^{P} \Delta p_{i,j} A_{i,j}, \qquad (10)$$

the force tending to increase d_2 is zero and the force tending to increase d_3 is

$$f_{3j} = -\sum_{i=1}^{P} \ell_{ij} \Delta p_{ij} A_{ij}, (a moment)$$
 (11)

where we assume that l_{ij} and r_{ij} carry the sign of their x-coordinate location. We will further assume that there are Q spanwise panel rows and P chordwise panel rows, implying that n, the dimension of $\{d\}$ is 3Q.

Let us now consider the computation of the normal wash W in terms of the displacements at the structural node points. By definition, the normal wash must be equal to the substantial derivative of the vertical displacement of the surface. (Implying no fluid flow through the surface.) In particular, we are interested in satisfying this boundary condition at the 3/4 chord points for each panel. The vertical displacement at any point along the chordwise centerline through node j

is
$$z_{j} = d_{1j} - xd_{3j}, \qquad (12)$$

where the definitions of Figure 7 have been used. The substantial derivative is therefore

$$W_{\mathbf{j}}(t) = \underline{D}(z_{\mathbf{j}}) = \overset{\circ}{d}_{\mathbf{i}\mathbf{j}} - xd_{3\mathbf{j}} - U_{\infty}d_{3\mathbf{j}}. \tag{13}$$

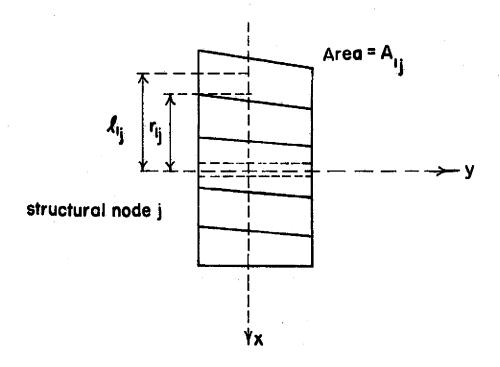


FIGURE 6. Span-wise slice of wing showing definition of symbols.

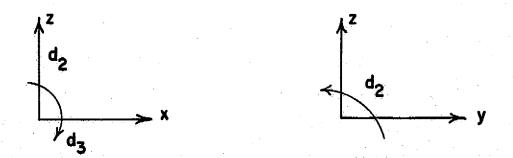


FIGURE 7. Definition of positive sense for displacements at node j.

Consequently, the downwash at the 3/4 chord of the ijth. panel can be written.

(Assuming no chordwise deformation).

$$W_{i,j}(t) = \overset{\circ}{d}_{i,j} - r_{i,j} \overset{\circ}{d}_{3,j} - U d_{3,j}. \tag{14}$$

Further, if W is assumed to be of exponential form,

$$W_{i,j}(t) = W_{i,j} e^{i\omega t},$$

(14) becomes

$$W_{i,i} = d_{i,i}(i\omega) - r_{i,i} d_{3,i}(i\omega) - U_{\infty} d_{3,i}$$
 (15)

Let us now return to (6) and establish the mechanism for computing the generalized nodal forces. Denote

$$\{w\} = \{w_{11} \ w_{12} \ \cdots \ w_{1Q} \ | \ w_{21} \ w_{22} \ \cdots \ w_{2Q} \ | \ \cdots \ | \ w_{P1} \ w_{P2} \ \cdots \ w_{PQ}\}^{T}$$

$$(16)$$

In (6), [D] is therefore a matrix of dimension PQ x PX. Let the force vector $\{f\}$, the pressure vector, $\{\Delta p\}$, etc. be defined using the same ordering as (16). In addition, let the generalized forces at node k be ordered as

 f_{1k} = vertical deformation force

f_{2k} = bending deformation moment

f = torsional deformation moment,

and define

$$\begin{cases} f \\ g \end{cases} = \{ f_{11} \ f_{21} \ f_{31} \ | \ f_{12} \ f_{22} \ f_{32} \ | \ \dots \ | \ f_{1Q} \ f_{2Q} \ f_{3Q} \},$$
 (17)

i.e., {f} denotes the vector of forces acting at the structural nodes. We must now develop appropriate transformation matrices so that {f} can be calculated in terms of nodal displacements {d}. From (10) and (11), we can write

$$3Q 3Q \times PQ PQ$$

$$\{r\}_{g} = [G] \{\Delta p\} (18)$$

where the matrix [G] is defined as

Equation (6) implies that

$$\{\Delta \mathbf{p}\} = \mathbf{q}_{\infty}[\mathbf{D}]^{-1} \{\mathbf{w}\}. \tag{20}$$

However (15) allows the following relation between {w} and {d}.

$$\{W\} = \frac{1}{U_{\infty}} [H] \{d\} + \frac{i\omega}{U_{\infty}} [E] \{d\}$$
 (21)

where [H] and [E] are defined by

$$\left\{ \begin{bmatrix} 1 & 0 & -r_{11} & 0 & 0 & 0 & \dots & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & -r_{12} & \dots & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & \dots & 1 & 0 & -r_{1Q} \\ 1 & 0 & -r_{21} & 0 & 0 & 0 & \dots & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & -r_{22} & \dots & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & \dots & 1 & 0 & -r_{2Q} \\ 1 & 0 & -r_{P1} & 0 & 0 & 0 & \dots & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & -r_{P2} & \dots & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & -r_{P2} & \dots & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & \dots & 1 & 0 & -r_{PQ} \end{bmatrix}$$

If we now combine (18), (20) and (21), we can finally write

$$\{f\}_{g} = \frac{q_{\infty}}{U_{m}} [G] [D(\omega)]^{-1} \{[H] + i\omega \{E]\} \{d\}$$
 (24)

C. The Static Aeroelasticity Problem

The bulk of the analytical work conducted during this study involved the estimation of elastic deformations under steady flow conditions. In this case, ω is set to zero in the aerodynamic matrices and D is defined over the field of real numbers. Hence (24) reduces to

$$\{\mathbf{f}\}_{\mathbf{g}} = \frac{\mathbf{q}_{\infty}}{\mathbf{U}_{\infty}} \left[\mathbf{G}\right] \left[\mathbf{D}\right]^{-1} \left[\mathbf{H}\right] \left\{\mathbf{d}\right\} \tag{25}$$

Gravitational loading of the wing was neglected because it was found that these forces were small compared to expected aerodynamic forces. The result of combining (25) with the composite stiffness matrix whose development was outlined in Section III-A is the following expression

[K] {d} =
$$\frac{q_{\infty}}{U_{\infty}}$$
 [G] [D]⁻¹ [H] ((d) + α {1}) (26)

where {1} is a vector of length 3Q each of whose components is a one. In effect, the term in parentheses on the right hand side of (26) contains a term dependent upon the elastic deformation {d} and a term dependent upon the rigid angle of attack, α. Now it is a simple manner to indicate the solution to (26), e.g.

$$\{d\} = ([K] - \frac{U_{\infty}}{Q_{\infty}} [G] [D]^{-1} [H])^{-1} \frac{Q_{\infty}}{U_{\infty}} [G] [D]^{-1} [H] \{1\} \alpha$$
 (27)

A computer program was written to implement (27) using the planar doublet lattice procedure (vortex lattice for steady flow) to calculate the deformed wing shape under a specified Mach number, q and rigid angle of attack, a. All theoretical aeroelasticity results described in Section IV of this report, were obtained via this procedure. A listing for this computer program is given in Appendix A.

D. Flutter Problem

The basic problem in flutter analysis is that of determining if the wing will develop oscillatory motions under test conditions. This requires the inclusion of appropriate mass matrices and an <u>unsteady aerodynamics</u> capability into the existing computer code).

By utilization of matrix structural analysis methods, discrete mass and stiffness matrices have been developed for the wing under consideration (See Section III). The resulting differential equation assumes the classical form

$$[M] \stackrel{\text{oo}}{\{d(t)\}} + [K] \{d(t)\} = \{F_{A}(t)\},$$
 (28)

where

[M] = mass matrix

[K] = stiffness matrix

 $\{d(t)\}\ =$ displacement vector for the structure

 $\{F_{\Lambda}(t)\}\ =$ the applied aerodynamic forces.

The basic approach was to ascertain those frequencies at which harmonic motion can exist as a solution to (28).

It is normally convenient in structural analysis applications to work with the frequencies and mode shapes associated with the unexcited structural system.

If we set $\{F_A(t)\}$ to zero in (28) and assume

$$\{d(t)\} = \{d\} e^{i\omega t}, \tag{29}$$

then (28) becomes, upon rearranging:

$$(\omega^2 I - [M]^{-1} [K]) \{a\} = \Theta$$
 (30)

It is clear therefore that the natural frequencies for the free system correspond to the eigenvalue of $[M]^{-1}$ [K] and mode shapes $\{d\}$ correspond to the eigenvectors of $[M]^{-1}$ [K]. Let us denote the eigenvalues by ω_i and the associated eigenvectors by $\{p_i\}$, where $i=1,2,\ldots,n$. (n is the dimension of $\{d\}$.) Define

$$[F] = [\{p_1\} \{p_2\} \dots \{p_n\}]$$
 (31)

$$[\Omega] = \operatorname{diagonal} \left[\omega_1^2 \omega_2^2 \dots \omega_n^2\right]. \tag{32}$$

The natural frequencies in radians per second are tabulated below:

Table - List of squared natural frequencies - (rad/sec)2

If we return to (28) and assume that the solution $\{d(t)\}$ is written as a linear combination of the basic vectors of [+] with time varying coefficient, we have

$$\{d(t)\} = \sum_{i=1}^{n} \phi_{i}(t) \{p_{i}\}$$
(33)

The $\phi_{\bf i}(t)$ are unknown scalar functions of time. We can place (33) into vector-matrix form by defining

$$\{\phi^{\text{T}}(t)\} = \{\phi_{t}(t) \cdot \phi_{2}(t) \dots \phi_{n}(t)\}$$
 (34)

and writing

$$\{\hat{\mathbf{d}}(\mathbf{t})\} = [\mathbf{P}] \{\phi(\mathbf{t})\} \tag{35}$$

The substitution of (35) into (28), with some manipulations, yields

$$\{\phi(t)\} + [\Omega] \{\phi(t)\} = [P]^{-1} [M]^{-1} \{F_A(t)\}.$$
 (36)

It follows therefore that by the introduction of the coordinates ϕ_i , $i=1, 2, \ldots, n$, the left hand side of (36) is decoupled and hence amenable to straight forward solution. However, the right hand side of (36), which has only been written in functional form to this point, is in fact a rather involved function of $\{d(t)\}$. With the substitution of (24) into (36), the dynamical equation for the elastic wing finally becomes:

$$\{-\omega^2 \mathbf{I} + [\Omega]\} \{\phi(\omega)\} = \{[S(\omega)] + i\omega[T(\omega)]\} \{\phi(\omega)\}$$
(37)

where $[S(\omega)] = \frac{q_{\infty}}{U_{\infty}} [P]^{-1} [M]^{-1} [G] [D(\omega)]^{-1} [H] [P]$ (38)

$$[T(\omega)] = \frac{q_{\infty}}{U_{\infty}} [P]^{-1} [M]^{-1} [G] [D(\omega)]^{-1} [E] [P].$$
 (39)

The inverse Fourier Transform of (37) is

$${}^{\circ \circ}_{\{\phi(t)\}} - [T(t)] * {}^{\circ}_{\{\phi(t)\}} + [\Omega] {}^{\{\phi(t)\}} - [S(t)] * {}^{\{\phi(t)\}} = 0$$
 (40)

where

$$[S(t)] = f^{-1} \{ [S(\omega)] \}$$
$$[T(t)] = f^{-1} \{ [T(\omega)] \}$$

and * denotes the convolution operation. The investigation for instability or sustained oscillation modes for the elastic wing is now reduced to that of finding the location of the roots for the characteristic equation of system (40). Unfortunately, closed form expressions are not available for the elements of [T(t)] and [S(t)] due to the fact that $[D(\omega)]$ can only be computed numerically for specified values of ω . Tests were made to determine if any of the lower natural frequencies corresponded to eigenvalues for (40) and it was determined that they áid not.

(IV) <u>Description</u> of <u>Tests</u>

Essentially two types of tests were conducted on the elastic wing after it had been fabricated at the Texas A&M Model Shop.

(A) Static Tests

The vortex lattice program was utilized to compute the aerodynamic loads that could be expected to act on each streamwise row of panels if the wing was rigid. The loads were computed for an angle of attack of 5° and $q_{\infty} = 80.1 \text{bs/ft.}^2$ Weights equal to these spanwise loads were attached to the 1/4 chord point for each panel section. Then vertical displacement measurements were made for each rib at 25% and 75% of rib length. By using these measurements and data on the unloaded wing position it was possible to calculate the wing elastic pitching rotation.

(B) Wind Tunnel Tests

A series of six wind tunnel tests were conducted at the Texas A&M University Wind Tunnel for two orbiter configurations. The conditions were:

$$q_{\infty} = 50 \text{ lb/ft}^2$$
; $\alpha = 2^{\circ}, 5^{\circ}, \& 8^{\circ}$
 $q_{\infty} = 80 \text{ lb/ft}^2$; $\alpha = 2^{\circ}, 5^{\circ}, \& 8^{\circ}$

The elevon setting was held at zero for all tests. These tests were conducted for the Orbiter with elastic wings and they were repeated for the Orbiter with

identical rigid wings. The standard force and moment data, C_L , C_D , and C_M , were recorded for each requence of tests. In addition, a Cathatometer was utilized to make vertical displacement measurements at each spanwise rib location for both the leading and trailing edges of the wing. The Cathatometer was instrumented with a potentiometer so that displacement readings could be automatically read into the wind tunnel digital computer. One difficulty that was experienced during the conduct of the test sequence was that the Cathatometer had to be moved in order to make both leading edge and trailing edge measurements. Due to the unevenness of the floor, the reference point was therefore shifted causing some difficulty in checking test repeatability.

(V) Comparison of Analytical and Experimental Results

As indicated in Section IV, a series of static load tests were conducted to verify that the structural model used for the wing in the computer program was in good agreement with the elastic deformations actually given by the wing. Figures 8 and 9 show curves of vertical deflection and elastic twist about the y axis derived from both experimental and analytical procedures. It is clear that good correlation was obtained for both twist and displacement in the static case, implying that the mathematical characterization of the wing was adequate.

Figures 10, 11, and 12 summarize some of the deformation and force data collected during the wind tunnet program. Figure 10 reflects the expected result that increased rigid angle of althock yielded increased z - direction deformations. Further, for a given \mathbf{q}_{∞} and α , α - deflections increased uniformly in going from the wing root to the wing tip. Figure 11 provides a comparison of $\mathbf{C}_{\mathbf{L}}$ for the elastic and rigid models obtained from experimental procedure. These curves are so close to rigid $\mathbf{C}_{\mathbf{L}}$ obtained from the analytical procedure that the latter has been omitted from the Figure. Finally, Figure 12 displays the elastic twist (increment in angle of attack) at α = 8 degrees for \mathbf{q}_{m} = 50 lb/ft² and 80 lb/ft². It is interesting to observe that a small negative

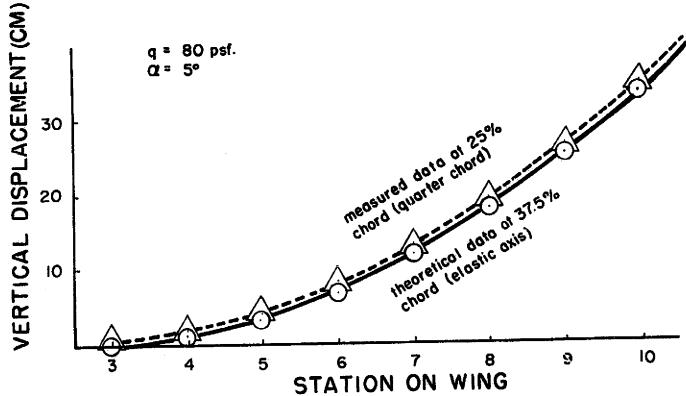


FIGURE 8. Comparison of the static load test linear deflections. Note that the deflection along the leading edge is in general larger than along the trailing edge.

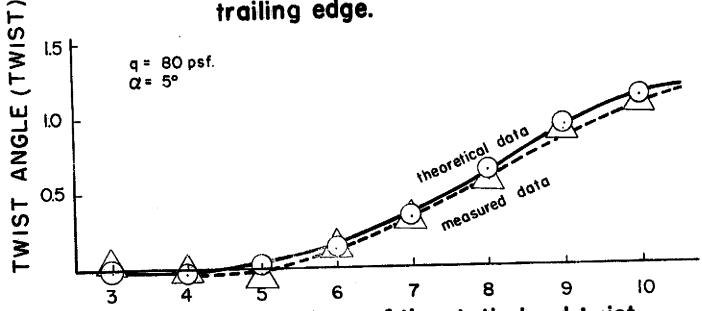


FIGURE 9. Comparison of the static load twist angle.

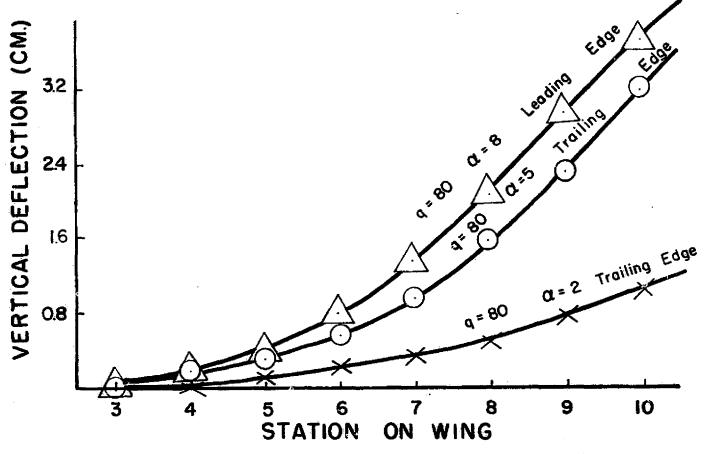


FIGURE 10. Plots of vertical deflections (in centimeters) measured in the wind tunnel.

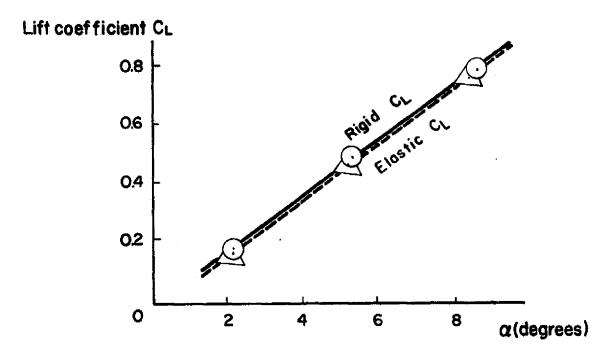


FIGURE II-a. Lift coefficient C_L versus angle of attack a, q=50 (leading edge).

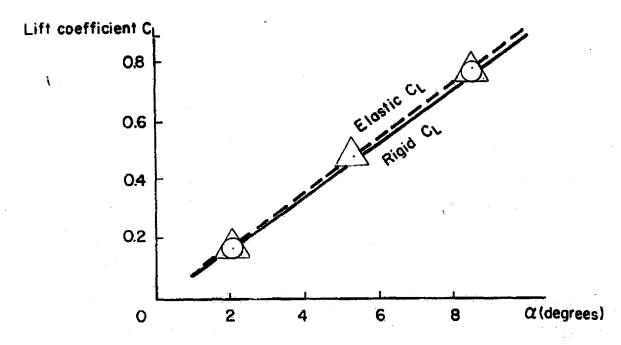


FIGURE II-b. Lift coefficient C_L versus angle of attack α , q = 80 (leading edge).

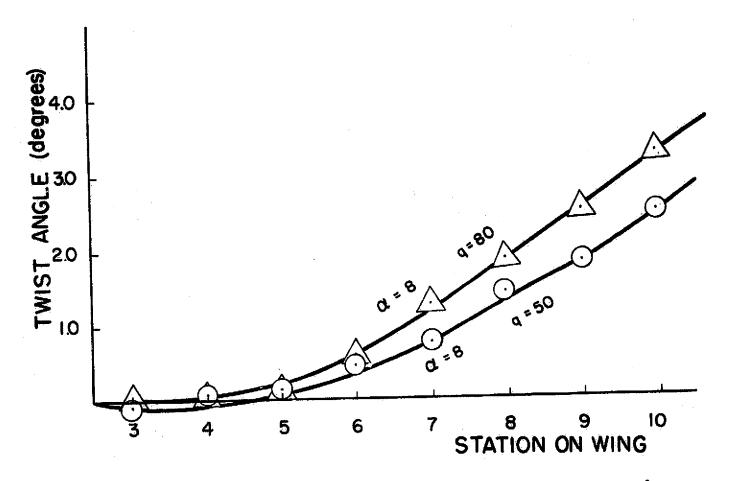


FIGURE 12. Plots of the twist angles measured from the wind tunnel.

angle of twist was measured at some of the inboard wing stations. Appendix B contains a tabulation of Wind Tunnel Test Results.

Finally, we wish to offer a comparison of experimental and theoretical aeroelastic estimates. The theoretical method outlined in Section III-C was used to estimate static aeroelasticity effects. The reader is reminded that the fuselage section of the orbiter was represented aerodynamically as a flat plate whose streamwise length corresponded to that of the wing root. Figure 13 shows a comparison of estimated and measurements for the wing leading edge z deflection. This Figure shows that this particular set of data correlated quite well. However, from Figure 14 we find that the theory estimates for elastic increment in angle of attack lie below those obtained experimentally. In an effort to determine if this difference was due to an inaccurate estimate of local center of pressure for each panel section, the centers of pressure were shifted forward by 20% and a new solution determined. While this does give better agreement, it does not appear that the solution to this discrepancy can be obtained by a simple center of pressure shift.

(VI) Discussion

In this report we have described the design, fabrication, testing, and analysis of a quasi-elastic orbiter model. The elasticity properties were introduced by constructing beam-like straight wings for the wind tunnel model. A standard influence coefficient mathematical model was used to estimate aeroelastic effects analytically. In general good agreement was obtained between the empirical and analytical estimates of the deformed shape. However in the static aeroelasticity case, we found that the physical wing exhibited less bending and more twist than was predicted by theory. Although the cause of this difference is yet unexplained, there are several factors that may have contributed to it:

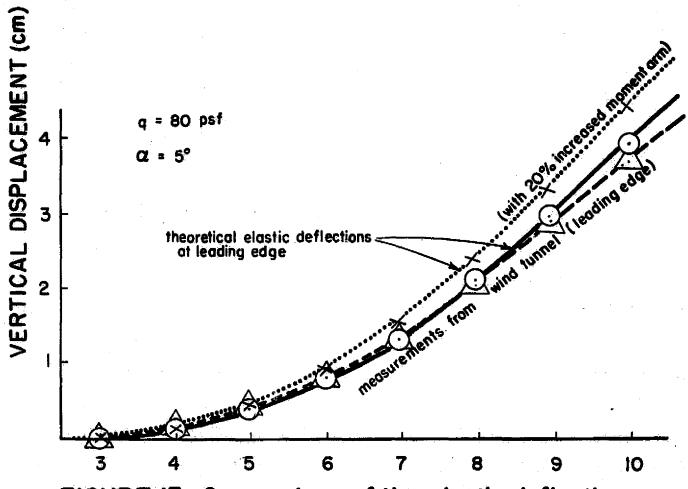


FIGURE 13. Comparison of the elastic deflections.

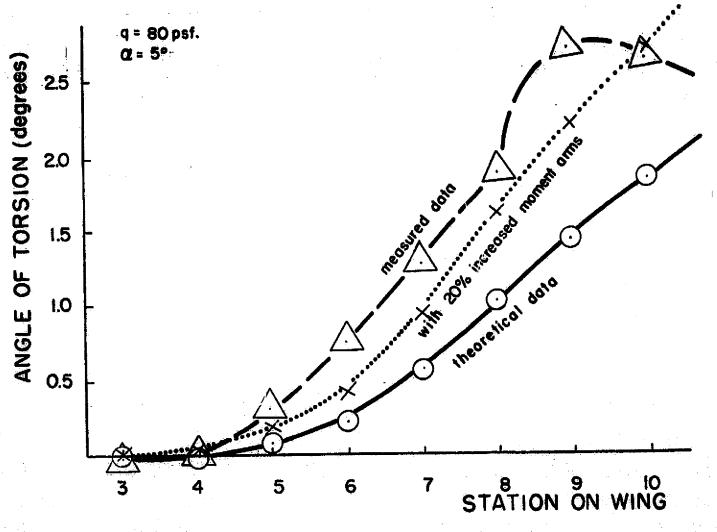


FIGURE 14. Comparison of twist angles.

- 1) Inadequate aerodynamic representation. (See above discussion)
- 2) Imprecise wind tunnel measurements. Although the wing was relatively quiet during testing some induced vibration occurred. This vibration along with cathatometer operator error almost certainly induced an unknown measurement error.
- 3) Structural Integrity. A continual problem that was experienced during testing was that the rib-spar weld joints could easily be destroyed by improper handling. This failure would explain spurious data points like the one at station 9 on Figure 14.
- 4) In-plane bending. The elastic wing was designed to have approximately the same stiffness in-plane as normal to the plane. Since the linear aerodynamic theory provides an inadequate representation for drag, it was not possible to adequately model this effect.

In summary, the results obtained in this report indicate that the linear aerodynamic and theories provide an approximate estimate of aeroelastic effects. However, our results imply that the theory <u>underestimates</u> (at least in this case) the elastic deformation in wing twist and hence the effects of elasticity on lift. We believe that further testing and more complete aerodynamic models are required to resolve this question.

References

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- [2] J. S. Przemieniecki, "Theory of Matrix Structural Analysis," McGraw-Hill Book Company, (1968).
- [3] J. P. Giesing, T. P. Kalman, and W. P. Rodden, "Subsonic Unsteady Aerodynamics for General Configurations," Technical Report AFFDL-TR-71-5, Part I, Vol. I, (1971).
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APPENDIX A

Aeroelasticity Computer Program Listing

The following pages centain a listing of the computer program used to compute the elastic displacements of the model wing.

```
//TB476
                JOB (1907-.4-C--. #10.001.C-). THISAYAKOPN
                                                                              JOB 958
     //*WATFIV
           **
                                   DISPLACEMENT ON MODEL WING
           **
                                     CAUSED BY DYNAMIC LOAD
               NOTATION
           PLSPAR(JI=LENGTH OF J-TH SPAR (INCH)
           MENUMBER OF SPANWISE PANELS
           MF=NUMBER OF DEGREES OF FREEDOM FOR EACH PANEL
           EDP(J)
                        =JTH. FLEMENT OF THE ELASTIC DISPLACEMENT VECTOR
           FDP(J)
                        #JTH. BLEMENT OF THE RIGID DISPLACEMENT VECTOR
           IMPLICIT REALER (4-H,D-7)
           DIMEMSTON ESTIFF(6.6).FSTIF1(6.6).STIFF(24.24).DIFF(24.24)
 3
           DIMENSION VECT (24), VECZ (24)
           BIMENSION E1(8), GJ(8), EDP(24), RDP(24)
           COMMON VAREALV RESPAR(8)
           COMMON /FREE2/
                                  THETAL
           COMMON /APEA3/ DINV(60.60).RIBUH(10).RIBLH(10)
           CCYMON 783:447 PERINV(48,601,A124,30)
 a
     С
        40 FORMAT (10F12.3)
10
        42 FORMAT (4X, 8515.5)
11
        44 FORMAT (3F15.6)
12
        46 FORMAT (T20+12)
13
        48 FD9MAT (8515.6)
        50 FERMAT (8-10.6)
14
15
        52 FCPMAT (9510.31
16
        54 FORMAT (8F15.5)
17
        70 FORMAT (*1*)
18
        72 FORMST (*-*)
19
        74 FORMAT (!-!.4x.!VALUES OF GJ (POUND-INCH SQUARED)!)
20
        76 FCPMAT (*-*,4x.*V2EUPS OF EI (POUNO-INCH SQUAREQ)*)
21
        78 FORMAT (!-!.4X.!LENGTH OF EACH SPAR (INCH)!)
        NO FORMAT ( -- + 4x + + 5LASTIC DISPLACEMENT VECTOR (ALONG THE MAJOR AXIS)
22
          1
23
        R2 FORMAT ("-",4X, "HERE IS THE STIFF-MATRIX")
24
        84 FORMAT ('-',T20, 'REDUCED SIZE OF D-INVERSE MATRIXI)
25
        86 FORMAT ('-'.T20.'/-MATRIX')
26
        BB FORMAT ("-".TZQ."MATRIX K- MATRIX A")
27
        91 FORMAT (7X. INCHI.T23. PADIANI.T37. PADIANI)
28
        94 FORMAT (4X+*ELASTIC DISPLACEMENT VECTOR (ALONG THE LEADING EDGE)*)
29
        95 FARMAT (7X. CENTIMETERS.,T22. DEGREES.,T37. DEGPES.)
30
        96 FORMAT (4X, "SLASTIC DISPLACEMENT (ALONG THE TRAILING EDGE)")
31
           8≄M
32
           MP2=M+2
33
           NF=6
34
           M3=(NF/2)44
35
          THETA1=0.16872
           CALL DLM (PET4.SO.ALPH4.N)
36
    ¢
           REDUCE INVERSE DEMATRIX TO THE WORKABLE SIZE
37
          MAMENM
```

38

MNT=1 "+ 21 = N

м

```
40
            12=0
           DO 890 J=1.N
41
42
           12=12+2
43
           00 890 T=1.P
            I J=I J+1
44
45
            12=12+1
           KL=0
46
4.7
           DO 888 L=1.N
48
            DO 888 K=1,MP2
49
           KL=KL+1
50
            SEDINALITYKE J=DINALIS*KF J
       888 CONTINUE
51
       RPO CONTINUE
52
53
            PRINT 94
54
           00 897 I=1,MN
55
           PRINT 46. I
           PRINT 42, (PFD MV(I, J), J=1, MNT)
56
57
       897 CONTINUE
58
           CALL AMAT (M.N.M3.ALPHA.SO, BETA.MSTAR)
           PRINTOUT THE A-MATRIX
59
            PRINT 86
           00 900 I=1,M3
60
61
           PRINT 46. I
           PRINT 40, (A(1,J),J=1,MSTAP)
62
       900 COMTINUE
63
     C
     C
            READ IN IMPUT-DATA
64
           RE40 52, (GJ(J),J=1,4)
65
           PEAD 52, (EI(J), J=1, M)
           READ 50, (RESPARIJ).J=1.M)
66
67
           DO 7 I=1.4
           GJ(I)=GJ(I)*1.120
68
69
         7 CONTINUE
     C
     C
           PPINT OUT INPUT-DATA
70
           PRINT 70
71
           PRINT 74
72
           PRINT 54. (GJ(J), J=1,M)
73
           PRINT 76
74
           PRINT 54. (EI(J).J=1.4)
           PRINT 78
75
           PPINT 48, (PLSPAR(J),J=1,M)
76
     Ċ
77
           DO 14 I=1.43
78
           DO 14 J=1.M3
79
        14 STIF=(1,J)=0.
80
           MM1 = M - 1
     C
     C
           FORM GLOPEL STIFFNESS AND MASS MATRICES
3 1
           DO 32 11=1.441
           I3M3=I1+3-3
3.7
           IF(II.GT.1160 TO 919
83
84
           CALL STIFFE (SSTIFL-GJ(1)-EI(1)-1(NF)
85
           CALL TREGRM (ESTIFIATHETA 1-NE)
34
           TALL STIFFE (SSTIFF, GJ(2), FI(2), 2,NF1
37
            CALL TREOSM (ESTIFF, THETA 1, NF)
```

39

ij≕ü

```
C
    99
               NE02=NE/2
    99
               DO 646 I=1.NFD2
    90
               DO 646 J=1,NFD2
    91
               ESTIFF (I,J)=ESTIFF(I,J)+E3 (IF1(I+NFD2,J+NFD2)
    92
           646 CONTINUE
    93
               GC TC 929
   94
           919 CONTINUE
    95
               1191=11+1
         C
    96
               CALL STIFFE (ESTIFF-GJ(11P1)-FI(11P1)-11P1-NF)
    67
               CALL TREORY (ESTIFF, THETA 1,NF)
    98
           929 CONTINUE
         C
               COMBINE ELEMENTAL MATRICES INTO GLOBAL MATRIX
    99
               00 13 JI=1.NF
   100
               DO IF KI=1.NF
               STIFF([343+J1.[343+K]]=STIFF([343+J1.[343+K])+ESTIFF(J1.K])
  101
  102
            13 CONTINUE
  103
            32 CONTINUE
         C
               PRINT OUT THE STIFF-MATRIX
  104
               PRINT B2
  105
               DO 280 I=1,43
   106
               PRINT 46. I
  107
               PRINT 54, (STIFF(I,J),J=1,M3)
  108
           280 CONTINUE
         C
               MATRIX K- MATRIX A
  109
               DO 310 I=1.43
  110
               03 310 J=1,43
               DIFF(I, J)=STIFF(I,J)-A(I,J)
  111
  112
           310 CONTINUE
  113
               6010 320
  114
               PRINT 88
**WARNING** UPNUMBERED EXECUTABLE STATEMENT FOLLOWS A TRANSFER
  115
               DO 311 I=1.43
  116
               PRINT 46, I
               PRINT 54, (DIFF(I,J),J=1,M3)
  117
  118
           311 CONTINUE
  119
           320 CONTINUE
         C
  120
               CALL INVIT (DIFF.M3.1.006)
               GENERALIZED DISPLACEMENTS
  121
               90 332 I=1.43
  122
               VEC2(1)=0.0
  123
               D7 332 J=1.MST/R
  124
               VEC2(I)=VEC2(I)+A(I,J)#ALPHA
  125
           332 COMTINUE
               07 360 T=1.M3
   126
  127
               SCP(11)=0.0
  128
               00 360 J=1.M3
  129
               EPP(I)=EDP(I)+BIFF(I,J)*VEC2(J)
  130
           360 CONTINUE
         C
               PRINT OUT DISPLACEMENT VECTOR
```

131

. . .

```
CIN OF MIC
```

```
PRINT RO
   132
              DRINT OF
  133
   134
              PR!NT 44, (EDP(L),L=1,M3)
   135
              PRINT 72
  136
              PRINT 94
  137
              PRINT 95
  133
              DO 400 I=1.M
  139
               J=[[-1] *3+1
  140
              K=(I-1) #3+2
  141
              L=(1-1) =3+3
              PPINT 44. FDP( 11*2.540
                                        +RIBUH(I )*EDP(L1*2.540
  142
                                                                    .EDP(K)*57.2
                    95780.EDP1L)*57.295780
*EXTENSION* OTHER COMPILERS MAY NOT ALLOW EXPRESSIONS IN OUTPUT LISTS
≠EXTENSIGN* OTHER COMPILERS MAY NOT ALLOW EXPRESSIONS IN DUTPUT LISTS
≠EXTENSION≠ OTHER COMPILERS MAY NOT ALLOW EXPRESSIONS IN OUTPUT LISTS
  143
          400 CONTINUE
  144
              PRINT 72
  145
              PRINT 96
              PRINT 95
  146
  147
              DO 420 I=1.M
  149
              J=(1-1) +3+1
  149
              K=11-11+3+2
  150
              L=(1-1) = 3+3
              PRINT 44. FOPt J1*2-540
                                      -RIBLH() 1*EDP(L)*2.540
                                                                    .FDP(K)*57.2
  151
                    95 "80: "DP(L1#57.295780
*EXTENSION* OTHER COMPILERS MAY NOT ALLOW EXPAGSSIONS IN OUTPUT LISTS
★EXTENSION★ OTHER COMPILERS MAY NOT ALLOW EXPRESSIONS IN OUTPUT LISTS
#EXTENSION# DTHER COMPILERS MAY NOT ALLOW EXPRESSIONS IN OUTPUT LISTS
          420 CONTINUE
   152
        Ċ
  153
           99 STOP
  154
              155
              SURROUTING DEV (PETA.SO.ALPHA.N)
        €
              THE DOUBLET LATTICE PROOFCURE
              FOR STEADY-PLANAF, SUBSCRIC. COMPPESSIBLE FLOW.
              INCREMENTAL OSCILLATORY COMNEASH FACTORS
              TBY FITTING THE KEEDEL FUNCTION FOR LIFTING FUNCTIONS WITH A PARABOLA)
              SYMBOLS:
                            ESTATIC AMBLE OF ATTACK
                    POSTLE-LOCATION OF THE POOT POINT ON LEADING SOGE
                    PECTTE=LEGATICS OF THE ROOT POINT ON TRAILING EDGE
                    TIPLE -LOCATION OF THE TIP POINT ON LEADING EDGE
                    TIPTS #UCCATION OF THE TIP POINT ON TRAILING BOGS
                          #MUMBER OF COLUMNS OF WING PANELS CON ONE WING!
                          HMUMPER OF PANELS PER COLUMN
                    (THE COLUMNS RUN FROM THE LEADING TO TRAILING EDGE DE THE WING)
                          =LENGTH CF SEMI-WING SPAN
                    PERCETTIEPSPORMTAGE OF CHOPOWISE LOCATION ON THE WING
                    PERCSIJI=PERCENTAGE OF SPAN-WISE LOCATION ON THE WING
                    MU(I.J)=LENGIH OF FACH DOUBLET LINE
                    DELACE JEAPEN OF SACH WING PANCE
                    XIII, J) = LOCATION OF EACH SENDING POINT ONT EACH PANEL
        C
                    X (1.J) = COCATION OF RECEIVING POINT ON EACH PANEL
                    AKSEP - SLOPE OF MAJOR AXIS OF THE WING
                    XIAX(3)=XI COORDINATES OF EACH COLLUMN ALONG THE MAJOR AXIS
```

ORIGINAL PAGE IS

```
DELCP(I)=PPESSURE COEFFICIENTS ON PME WING
                  V۸
                           -SPEED OF SOUND
                           SEPRET STREAM MACH NUMBER
                  FMACH
                  UINE
                           FREE STREAM
                                              VEFUCITA
      C
            IMPLICAT REALMR (A-H.D-Z)
156
                                       PCVSLP(A), SLOPF(A), PERCS(11), PEPCC(7)
            DIMENSION
157
158
            DIMENSION XIIP (6),XIOR(6),XIID(61,XIDD(61,TANLAM(7)
            nivensing xii(7).xin(7).y(10).eTAC(10).xiAX(16).C(11).ETAC(11)
159
            DIMENSION X1(6,10),XIC(6,10),X(6,10)
160
                                  DFLP(6,10), DFLX(6,10),
            DIMENSION
                                                                  R(6.101
161
162
            DIMENSION DELC(6,11)
            REAL*8 LIMOICA F. LAMBAD(5), MU(6, 10), ILEFT, IRIGHT
163
164
            COMMON /ARTA3/ DRSS(60.60).RIRUH(10).RIBLH(10)
            COMMON /48(15/ OFLA(6,10),FL (6,10)
165
        200 READ (5.210.END=990) ROOTLE.ROOTTE,TIPLE.TIPTE.B.N. M.ALPHA
165
1.67
        210 FC@MAT (5F10.3.2110.F10.6)
168
            PRINT 220
        220 FORMAT ('11') '
169
1.70
            PRINT 230
        230 FORMAT (4X. DATA INPUT: - 1)
171
            PRINT 240, ROOTLE-FOOTTE-TIPLE-TIPTE-R-M-M
172
        240 FORWAT (4X.*ROFTEE= *.FIG.4.4X.*ROBTTE= *.F1G.4.4X.*TIPLE= *.F1G.4
173
                   ,4X,*TIPTE= *,Fl0.4,4X,*B= *,Fl0.4,4X,*M= *,I4.4X,*K= *,I4.
174
            PRINT 250, FLPHA
        250 FORMAT (1-1,4x, ANGLE OF ATTACK IS 1,F10.6)
175
      C
176
            VA=1090.0
177
            W=0.0
178
            Px=0.0
179
            UIMF=250.0
180
            FM4CH=UINF/VA
.81
            BFT4=0SQRT(1.0-FM4CH**2)
195
            B=9=BETA
             $9=0.50#0.002503867*UINF**2
183
194
            PRINT 252, FMACH, RETA, SO
        252 FORMAT (T2D, *MACH NUMBER=*, F10.6, T60, *8FTA=*, F10.6, T90, *DYNAMIC PR
185
           1ESSURE, 0=1.F10.31
      C
             PRECALCULATION FOR THE COOPDINATES OF THE SENDING AND RECEIVING ELEMENTS
      C
            CALCULATION OF THE AREA OF EACH WING PANEL
186
             IN=N+1
            [M=M+1
187
            体化性が生物
188
            PEAC 254, (PERCS(J), J=1, IM)
189
190
            A980 254, (PERCC[I], I=], IN)
191
        254 FORMAT (8F10.5)
192
             PRINT 258
        258 FORMAT ('-'.4X. PEPCENT OF SPANWISE PANELING LOCATION')
193
196
            PRINT 305, IPEPCS(J).J=1.IM)
195
             PRINT 260
        260 FORMAT ("-".4X. PERCENT OF CHORDWISE PANELING LOCATION")
196
197
             PRINT 305, (PEFCC(II,I=1,IN)
198
            ED 270 J=1,14
            (U) 20 AFFEFF = (U) 173
199
        270 CONTINUE
200
             DC 280 T=1.IN
201
202
             XII(I)=(2007TE-ROOTLE)*PERCC(I)+ROOTLE
```

```
203
            XID(I)=(TIPTC+TIPLE)*PEPCC(II+TIPLE
264
            TANLAM(I)=(X17(I)-XII(I))/8
205
        280 CONTINUE
206
            C(1)=ROCTT -RIGILE
207
            CIIMI=TIPTE-TIPLE
209
            AXSLP=(TIPLE-ACOTLE+0.3750*(C(IM)-C(1)))/8
209
            AXDEG=57.255780*DATAN(AXSLP)
210
            PRINT 284. AXDES
211
        284 FORMAT ('-'.'SLOPE OF MAJOR AXIS =1.F16.6.1 DEGREES*1
      C
      C
            SLOPE OF LIME COURLETS, SLOPE, WITH ITS ANGLE, LANDA.
212
            00 370 I=1 .N
213
            00 300 J=1.IM
214
            C(J)=C(1)-(C(1)-C'IM))*PFRCS(J)
215
            OELC(I, J)=(PFRCC(I+1)-PFRCC(I))*C(J)
216
        300 CONTINUE
217
            XIID(I)=XII(I)+0.250 *DELC(I.1)
218
            XIDP(I)=XIC(I)+0.250*DELC(I.IM)
219
            SLOPE(1)=(x1^0)111-x110(11)/8
220
            LAMBA(I)=DATAM(SLCPE(I))
221
            LAMBAD( [] = LAMBA([] +57.296780
222
            XIIR([]=XII (I)+0.750 *0FLC([.1]
            XIOP(I)=XIC(I)+0.750 = 0FLC(I,IM)
223
        370 RCVSLP(II=(XIOF(I)-XIIR(I))/8
224
225
            PPINT 390
226
        380 FORMAT (!-!.4X: ANGLE OF PACH DOUBLET LINE (IN DEGREES)!)
227
            PRINT 305. (LANDAD(1).1=1.N)
228
        305 FORMAT (4X,F16.6)
      ¢
      C
            NOW COMPUTING THE REQUIRED COORDINATES
229
            IJ=0
230
            DO 405 I=1,N
231
            DO 405 J=1.4
232
            MU(I.J)=(ETA(J+1)-ETA(J))/DCOS(LAMDA(I))
233
            INDEX J= 2 = ("-J]+1
            DELA(I, J)=0.50E0=0ELC(I, )) * (FTA(J+1)-ETA(J)) * (C(1) * INDEXJ
234
                   +0(IM)*(2*3-13)/(C(1)*M)
235
            DELACT, J)=DELACT, J)/SETA
            11=11+1
236
237
            XI(Tau) =XIID(I)+FTA(J ) PSLOPE(I)
238
            ETACIJI=0.50*(FTA(J)+ETA(J+1))
239
            Y(J)=ETAC(J)
240
            X([,J)=XII*([)+2CVSLP([]+Y{J})
241
            DELX(1, M=0.50=(PELE(1,J)+DELC(1,J+1))
242
            XIC(I.J)=X(I.J)-0.50=0ELX(I.J)
            X(AX(J)=0.375J=0(1)+AXSLP+Y(J)+ROOTLE
243
244
            FL(I,J)=XIC(I,J)=XIAX(J)
            f(I,J) = x(I,J) - x(Ax(J))
245
            PIBUH(J)=(C(J)+C(J+1))/2.0*0.3750
246
247
            FIP(H(31=919U4(J)±0.6250/0.3750
        405 CONTINUE
248
249
             PPINT 308
        BOBLECRMAT. (!-!, 'XI-LOCATIONS ALONG THE MAJOR AXIS:-!)
250
251
            PPINT 340, (XIAX(K),K=1,M)
252
             PRINT 310
        310 FORMAT ("-",4X, "HERE IS THE VECTOR OF ME
253
            DR 311 H=1.00
254
255
             PRINT 330
256
             ORINT 34D, (NUCL, J),J=l,K)
```

TOWN PAGE IS

<u>~</u>

```
257
        311 CONTINUE
             PPINT 314
      C 314 FORMAT (*-*,4X,*X-LOCATIONS OF EACH RECEIVING POINT*)
             PRINT SEG
             PRINT 340, ((X11,J),J=1.M), I=1.N)
259
             PPINT 320
259
        320 FORMAT ('-',4x, 'PANEL AREA ON ONE WING')
260
             00 350 I=1.N
             PPINT 330
261
262
        330 FCPMAT ('-')
263
             PRINT 340, INCLAIL, JI, J=1, MI
264
        340 FORMAT [4X.]0F12.61
265
        350 CONTINUE
             PRINT 352
266
267
         352 FORMAT ("-",T20,"L(1,J) WITH SIGN OF THEIR X-COORDINATE LOCATION 8
            TEING CAPRIED ALONG! I
268
             00 353 I=1.N
             PPINT 330
269
             PRINT 340. (FL(I.J).J=1.M)
270
271
        353 CONTINUE
             PRINT 354
272
        354 FORMAT (*-*,T29,*R(I,J) WITH SIGN OF THEIR X-COORDINATE LOCATION 8
273
            TEING CARRIED ALONG!
274
             DG 355 I=1.N
275
             PRINT 330
             PPINT 340, (P(I.J),J=1.M)
276
277
        355 CONTINUE
      C
             NOW CALCULATE DRS(1) AND DRS(5) MATRICES
             PRINT 360
      C 360 FORMAT ( -1.19X. DASS -20X. DRS1 1)
278
             T1=1.0
279
             K F=0
             DO 590 K=1.N
280
281
             DO 590 L=1.4
282
             KL=KL+L
293
             IJ=0
             PPINT 415
      C 415 FORMAT (*-*)
             PRINT 363, KL
284
             DD 580 I=1.N
             PRINT 315
      C 315 FORMAT (4X."
                              1)
285
             DO 580 J=1.™
286
             1.j=1.J+1
287
             X^{\dagger}X^{\dagger}=X^{\dagger}K_{\bullet}L_{\bullet}-X^{\dagger}\{I_{\bullet}J\}
289
            YMETA=
                       (LIATE-(J)Y
289
             YPPTA=Y(L)+6T4(J)
290
             XMXIC=X4K*f3-XIC(I*A)
             VMETAC=
291
                        YIL)-FTAC(J)
292
             YPETAC=Y(L)+FT/C(J)
            REOT= DSOTTING(I.J)**?-2.0 *(XMXI*DSIN(LAMDA(I))
293
                   +YMETA+DCOS(L&MD4(I)))+MU(I,J)+XMXI++2+YMETA++2)
294
             IRIGHT=MU(I,J)/(YMFT3+(Y(L)-ETA(J+1)))+(ROOT/(Y(L)-ETA(J+1))
                   - PSOPT (X/XX [4+2+YHET 4+2)/YMETA)/(XMXI+DCGS(LAMDA(I))
                   -YMETA #D SINTLAMDA(I)))
             REGT= DS021(#4)([.J)**2-2:0 *(XMXI*0SIN(LAMDA([]))
295
                   -YPSTA=OCOS(LAMDA(I)) }*MUTI.J)+XMXI**2+YPETA**2}
296
             ILSFT=MU(I,J)/(YPSTA*(Y(L)+STA(J+1)))-(ROOT/(Y(L)+STA(J+1))
                   - DSORTIXMXI*=2+YPETA +=21/YPETA 1/(XMXI*OCOSTLAMDATI)1
```

```
2
                   +YPETA+DSIN(LAMDA(III)
      C
            DRSS=(IRIGHT+ILFFT)*DCOS(LAMDA(I))
            IF (W.EQ.O.O) COTO 492
            DRSS(KL.IJ) = (IPIGHT+ILEFT) = CCOS(LAMDA(I))
297
298
            0°55(KL.IJ)=0RSS(KL.IJ)*0.50*DELX(I.J)/4.0/3.14159265360
            TRANSFORM BACK TO THE ORIGINAL Y-AXIS
      C
299
            YMETA=YMETA/RETA
            YPETA=YPETA/BETA
300
            YMTTAC=YMETAC/RETA
301
302
            YPETAC=YPETAC/RETA
303
        580 CONTINUE
        590 CONTINUE
304
      C
305
            CALL INVPT (PRSS, MN, 1, 000)
      C .
306
            DO 600 I=1.N
307
            DO 600 J=1.M
309
            FL (I.J)=FL (I.J)/95TA
        600 CONTINUE
304
            GOTO 200
310
        990 COMTINUE
311
            RETURN
312
313
            =N0
      C
314
            SUPPOUTING STIFFE (ESTIFF.EGJ.EFI.N.NF)
315
            IMPLICIT REALER (A-H,O-Z)
316
            DIMENSION PSTIFF(NF+NF)
317
            COMMON MAREALA RESPARCAL
      C.
319
            PIC =FLSPAR(N)
319
            FLC2=PLC**2
320
            PLC3=RLC**3
            FORM SEMPING STIFFNESS MATRIX -
            26 40 I=1.4F
321
            TE 40 J=1.NE
322
323
            ESTIFF([,.1)=0.0
324
         40 CENTIBUE
325
            FSTIFF(1,1)=12./RLC?*EEI
325
            FST1FF41+21=6./RLC2*FF1
727
            FSTIFF(1,4)=+12./RLC3#EFI
224
            ESTIFF(1.5)=6./PLC?**FI
370
            ESTIFFICATION ESTIFF(1.2)
330
            FSTIFF(2.2)=4. /FLC+FEI
331
            ESTIFFIC.4)=+6./RLC2*SEI
332
            ESTIFF(2,5)=2./?LC#EEL
333
            ESTIFF(4.1)=ESTIFF(1.4)
3.4
            ESTIFF(4,2)=ESTIFF(2,4)
335
            FSTIFF(4,4)=FSTIFF(1,1)
335
            ESTIFF(4.5)=-6./#LC2#66T
277
            ESTIFF(5,1)=ESTIFF(1,5)
338
            ESTIFF(5-2)=[STIFF(2.5)
339
            ESTIFF(5,4)=[STIFF(4,5]
            ESTIFF(5,5)=ESTIFF(2,2)
343
      С
            FORM TORSIONAL STIEFNESS MATRIX-
34:
            FSTIFF(3,3)=EGJ/RLC
342
            FSTIFF(6.3)=-EGU/RLC
```

```
ESTIFF(3.6)=ESTIFF(6.3)
343
344
             ESTIFF(6.6)=ESTIFF(3.3)
345
             RETURN
             FND
346
      C
347
             SUBROUTINE TREORM (A.THETAT.NE)
348
             IMPLICIT REAL=8 (A-H.O-Z)
349
             DIMENSION A(NE.NE). TRANS (6 .6 ). PROD(6 .6 )
350
            DB 44 1=1.NF
351
             DO 44 J=1.8F
352
         44 TRANS(I.J)=0.0
353
             TPANS{1.1}=1.0
354
             TRANS (4.4)=1.0
355
            TPANS(2.2)=OCOS(THETAT)
356
             TRANSIZ.31=+DSINCTHETATE
357
             TFAMS(3.2)=DSIN(THETAT)
352
             TRANS(3.3)=000S(THETAT)
359
            TPANS(5.5)=DCGS(THETAT)
360
             TRANS(5.6) =- DSIN(THETAT)
361
             TRANSIG.51= DSINITHETATI
             TEAMS(5.6)=DCOSCTMETATE
352
             DP 51 I=1.NF
363
             DU 51 J=1.NF
364
365
             PFOD(I.J)=0.
            PO 52 K=1.NE
366
         52 PRODUITURE PRODUITURE TRANS(K.11*A(K.J)
367
368
         51 CONTINUE
            DD 53 I=1.NF
359
370
            DO 53 J=1.NF
371
            A([,J)=0.0
372
             00 54 K=1.NF
                                (I,J)+PROC(I,K)*TRANS(K,J)
373
         54 A
                   \{I,J\}=\Delta
374
         53 CONTINUE
            EFFUEN
375
376
             END
377
             SUBROUTINE AMAT (M.N.H3.ALPHA.SO. PETA.HSTAR)
             SYMBOLS:-
      €
            THE TAIL
                          = A'IGLE FROM ELASTIC AXIS ONTO THE Y-AXIS'
             THE TAZ
                          =ANGLE FROM LINE OF LOADINGS ENTO THE Y-AXIS
                          = SEMI-SPANNISE LENGTH
                          #LOCATION OF THE ROOT POINT ON LEADING FOGE
            RUCTLE
            POOTTE
                          -LOCATION OF THE POOT POINT ON TRAILING EDGE
      ٤
            TIPLE
                          = EDCATION OF THE TIP POINT ON LEADING EDGE
            TIPTE
                          #LOCATION OF THE TIP POINT ON TRAILING EDGE
            PATREG
                          EARIGLE OF ATTACK IN DEGREES
            EXF(L1)
                          =VERTICAL FORCE LOAD ONTO THE J-TH. SECTION OF THE WING
      C
      C
            FXF(L2)
                          #HENDING KOMENT LOAD ONTO THE WING LEGUALS ZERO IN MERCI
      ¢
            EXF(L3)
                          STORISIONAL MOMENT LOAD ONTO THE USTH. SECTION OF THE WING
                           (CAUSED BY VERTICAL FORCE APPLIED OFF FROM THE MAJOR AXIS)
                          =Y-LOCATION OF EACH WING SECTION
            Y(.))
            XZX(J)
                          = X-LOCATION ALONG THE MAJOR AXIS
            XLD(J)
                          EXHLUCATION ALONG THE LINE OF LOADING ON THE WING
            AFMUJI
                          = TOR STONAL MOMENT ARM OF THE U-THE SECTION
            R.I. C
                       -- "SPAUWISE LENGTH OF EACH PANEL
            FF (I.J)
                          =CONDENSED CIRCULATION MATRIX
```

```
C
             DPC (J1)
                           =DISTANCE OF DYNAMIC PRESSURE OFF FROM THE MAJOR AXIS
      Ç
373
             IMPLICAT PEALER (A-H.O-Z)
             DIMENSION ETAIMPLE
379
             DIMENSION ETA(9). OPC(8). FLD(48)
390
             DIMENSION ARMISH-FOR.101.
                                            XAX(8),XLD(8),Y(8)
381
             DIMPNSION
                                 CLA( 8.10).DEL CP(48.10)
392
             COMMON JAMEAS/
                                     THETAL
             COMMON /AGEA4/ REDINV(48,601,A(24,30)
343
             FCMMON /AREAS/ DELA(6,10), FL (6,10) -
384
           2 FCPMAT (RF10.6)
385
386.
           8 FORMAT ("-",4X,"ACTUAL MOMENT ARM OF EACH COLUMN (ALONG THE SPAN)"
      C
387
             THETA2=0.20362
388
             PROTILE = 0.0
389
            PORTIF=10.0050
390
             TIPTE=10.0050
             TIPL#=5.980
391
             R=21.80
392
            CALCULATE DISTANCE OFF FROM THE MAJOR AXIS OF EACH STATION
393
             4P1=4+1
             *P?="+?
304
395
             WSTAR = PR+6
369
             DC 30 J=1,491
            型 TA ( J ) = R市 ( J-1 ) / M
397
          30 CONTENUE
39A
369
            00.40 J=1.7
             Y(J)=0.50*(CTA(J)+5TA(J+1))
400
             * Axial=RCCTLE+0.3750*(FCOTTE-ROCTLE)+Y(J)*OTAN(THSTA1)
401
             X LP(J)=800TLE+0.250 *(RCGTTE+ROOTLE)4Y(J)=0TAN(THETA2)
402
             ## (J) = X 0 X(J) - X LD(J)
403
         40 CONTINUE
474
            地名中华阿
405
             DO 43 I=1.4NN
40%
             70 43 J=1.MP2
407
408
            DEL CP([,J)=0.0
            99 42 K=1.1
409
410
             L=44-11 AMP2
            TIL CP(I.J) =BEL CP(I.J)-RED INV(I.J+L)
411
         43 CONTINUE
412
         43 CONTINUE
413
            DO 45 I=1.M
414
            P.C. 45 J=1,MP2
415
            Ct:(I.J)=0.0
416
417
             30 44 K=1.社
            (= (Y-?) *M
413
419
            CLA(I.1)=GLA(I.J)+DEL EP(I+L.J)/BETA*DELA(K.I+2)
         44 CONTINUE
420
            F ([+J}=CLA([+J)*SQ/144.0
421
         45 CONTINUE
422
      €
             FIND THE EXACT LOCATION OF DYNAMIC PRESSURE
            いだもく = MPコキリ
423
            PC 60 1=1.8%
424
            FLQfIl=0.0
425
             00 60 J=1.MNFS
426
             FUSITI = FUSITI - REDINVII.JI
427
```

H

```
428
         60 CONTINUE
429
            DO 65 J=1.M
            REP1=0.0
430
            FFP2=0.0
431
432
            DO 62 J=1.N
            K=11-11*M+J
433
434
            FLO(K)=FLO(K)*CELA(I+J+2)/BSTA
435
            FLD(K)=FLD(K)+57/144.0
            PEP1=REP1+FLD(K)
436
            REP2=RFP2-FL(I+J+2)*FLD(K)
437
         62 CONTINUE
438
            DPC(J)=REP2/FEF1
439
440
            PPC(J)=PPC(J)*1.20
         65 CONTINUE
441
      C
      C
            PRINT OUT THE MOMENT ARM
442
            PRINT 8
            PRINT 2, (BPC(J), J=1,M)
443
            COMPARE TO THE QUATER CHORD MOMENT ARM
            PRINT 2, [AHMIJ], J=1,4]
444
            FORM COSFFICIENT MATRIX FOR EXTERNAL LOAD
            22 50 1=1,43
445
            00 50 J=1, "STAP
446
447
             0.0=(L.T12
          SO CONTINUE
448
             0° 55 1=1.8
449
            #FM(I)=CPC(I)
450
451
            | 7= [ × ]
452
            DC 55 J=1-MP2
             J3=J*3
453
454
            A(13-2, J3)=F(1,1)
455
            # (!?,J3)=F(I,J)*ARM(I)*PCGS(ALPHA)
          55 CONTINUE
456
            ラピエ. IC No
457
458
             SUPPOUTING INVETIGANASCALED
459
             IMPLICIT PEAL#8 (7-H.O-Z)
460
            DIMENSION A(M.A), INDEX (90, 23, IPVOT(90), PIVOT(90)
441
            CALL *RRS#T(207,256,0,1)
      C
             SCILE DOWN MATRIX A
462
            0.7 \text{ I} I=1.N
            DD 1 J=1.N
46?
          1 A(T,J)=A(T,J)/SCALE
464
            053=1.0
455
             7199=0.0
466
          57 BET = 1 NE
457
458
             35 17 J=1.N
459
          C=1 L) TOVOT 131=0
            DC 135 I=1.N
470
            POLEMBLY 12 STATEMENTS FOR SEARCH FOR TIVOT ELEMENT
             T=7580
471
             37 G ##1.5
472
             14(19717(3)+1) 12:44:13
473
          13 77 23 4-1,5
474
475
             TF([PVCT(K)-1) 43,23,91
```

V

```
43 IF10ARS(T)-DABS(AfJ,K))) 83,23,23
  476
  477
            83 IFOW=J
  478
               ICOL=K
               T=4(J.K)
  479
            23 CHATIMUS
  480
             9 CENTINUE
  481
               IPVOT(ICOL)=IPVOT(ICOL)+L 1
  482
               FOLLOWING 15 STATEMENTS PUT PIVOL ELEMENT ON DIAGONAL
  483
               TECTROW-TOOL) 78,109,73
   494
            73 DET=-PET
               DO IS L=1.7
   4R5
               THATTEGER L
  496
   487
               ATTROWALD = ATTECLAL
            12 A(ICTL, L)=T
  488
           109 INDEX[[,1]=[PAN
  489
               If DEX(I.2) = ICOL
  490
               PIVOT(I)=4(ICOL, ICOL)
  491
  492
               DET=DEF=PIVOT(!)
               FOR CHING 6 STATEMENTS TO DIVIDE POVOT FOR BY PIVOT BLEMENT
         C
  493
               Affort, Kort Ferme
               DC 205 L=1.9
   404
           205 ATTCCL.L)=*(ICCL,L)/PIVOT(I)
   495
               FOLLOWING TO STATEMENTS TO REDUCE NON-PIVOT ROWS
               00 125 Alalah
  496
               MF(LI-100t) 21,135,21
  497
           ·21 T=3{| T.ICOL}
  408
               ATLI-ICOL)=ZERO
   499
               OC 89 L=1.4
   500
            89 A(L1-1)=A(L1-L)-A(100L+L)*T
   501
           135 CONTINUE
   502
               FOLLOWING 11 STATEMENTS TO INTERCHANGE COLUMNS
   503
           222 00 3 1=1.4
  504
               1 = 1 - 1 + 1
               IF(IMO) ((E,1)-INDEX(E,2)) 19,3,19
  505
            19 JETH#TND-X(L,1)
   506
               JCCL=15.05X(: +21
   537
   508
               DO 549 KELON
               T=4(8,520m)
   509
  510
               A(K, JROW) = 1 (K, JCOL)
   511
               # (K.USOL) * T
   512
           549 CCNTINU"
             3 CENTIME
  513
            BL CONTINUE
  514
               SCALE BACK INVERSE OF MATRIX-A
               30 2 I=1.N
  515
               00 2 J=1.5
  516
   517
             2 A() J)=A(T,J)/SCALE
  518
               RETURN
           AI PETURN
               END
   519
         1/476TA
***#GRRCR*** INSUFFICIENT MEMORY TO ASSIGN ARRAY STOFAGE. JOB ABANCOMED
                              26312 BYTES.APRAY AFEA= 82752 BYTES.TOTAL AFEA KVAILABLE= 104544
```

I. NUMBER OF MERNINGS=

0.00 550.

1. NUMBER OF EXTENSIONS=

TAMU/WATEIV - VER 1 LEV 3 JANUARY 1972

neueor coos∍

NUMBER OF SPROKS=

6.69 SEC.EX COTTON TIME=

COSE USAGE

DIAGNOSTICS COUPILE TIME =

DATE= 74/217

APPENDIX B
Tabulation of Wind Tunnel Data

 $S_{REF} = 423.06 \text{ sq. in.,}$ $\bar{C} = 8.36 \text{ in.}$

I) q_∞= 50

LEADING EDGE	STATION NUMBER	VERTICAL DEFLECTION	
$\alpha = 2.13$	ON WING	δ _{LE}	$\delta_{ ext{TE}}$
c _{r.} = 0.1683	3	0.007	-0.015
$c_{\rm D} = 0.1037$	14	0.036	-0.015
$C_{PM} = -0.1684$	5	0.083	0.042
TRAILING EDGE	6	0.176	0.196
$\alpha = 2.13$	7	0.301	0.239
C _{T.} = 0.1679	8	0.45	0.301
c _D = 0.1016	9	0.584	0.486
C _{PM} = -0.1635	10	0.731	0.682

LEADING EDGE	STATION NUMBER	VERTICAL DEFLECTION	
α = 5.37	ON WING	δ _{LE}	δ _{TE}
$c_{L} = 0.461$	3	-0,029	0.028
$c_{D} = 0.1215$	4	0.064	0.079
C _{PM} = -0.3301	5	0.21	0.163
TRAILING EDGE	6	0.442	0.379
a = 5.37	7	0.752	0.662
$c_{T_{i}} = 0.4675$	8	1.174	0.985
$C_{D} = 0.1242$	9	1.617	1.456
C _{PM} = -0.3341	10	2.096	2.005

LEADING EDGE	STATION NUMBER	VERTICAL DEFLECTION	
$\alpha = 8.61$	on wing	δ _{LE}	δ _{TE}
c _L = 0.758	3	0.021	0.058
C _D = 0.1495	4	0.19	0.163
C _{PM} = -0.4591	5	0.442	0.395
TRAILING EDGE	6	0,849	0.71
a = 8.6	7	1.406	1.182
C _L = 0.7521	8	2.089	1.724
$C_{\rm D} = 0.1505$	9	2.905	2.491
C _{PM} = -0.4552	10	3.742	3.258

II) q_∞= 80

LEADING EDGE	STATION NUMBER	VERTICAL DEFLECTION	
$\alpha = 2.13$	ON WING	δ _{LE}	δ _{TE}
$c_{L} = 0.1676$	3	0.021	-0.22
$c_{\rm D} = 0.1059$	<u>.</u>	0.064	0.035
C _{PM} = -0.1671	5	0.132	0.098
		0.282	0.203
TRAILING EDGE	6	, 0.202	}
$\alpha = 2.13$	7	0.1463	0.324
$c_{i} = 0.167$	8	0.718	0.457
c _D = 0.1033	9	0.908	0.747
C _{PM} = -0.1665	10	1.175	1.019

LEADING EDGE	STATION NUMBER	VERTICAL DEFLECTION	
α = 5.38	ON WING	, ⁶ LE	δ _{TE}
$C_{L} = 0.4779$	3	0	0.02
C _D = 0.1254	ļţ	0.149	0.155
C _{PM} = -0.3443	5	0.408	0.296
TRAILING EDGE	6	0.78	0.535
α = 5.38	7	1.323	0.95
C _L = 0.4759	8	2.048	1.562
C _D = 0.1252	9	2.898	2.286
C _{PM} = -0.3437	10	3.678	3.165

LEADING EDGE	STATION NUMBER	VERTICAL DEFLECTION	
α = 8.62	ON WING	δ _{LE}	$\delta_{ ext{TE}}$.
C _L = 0.7728	3	0.048	0.037
C _D = 0.1540	ъ.	0.268	0.236
$c_{PM} = -0.4776$	5	0.639	0.591
TRAILING EDGE	6	1.335	1.153
a = 8.62	7	2.251	1.891
$c_{L} = 0.7732$	8	3.356	2.87
$c_{\rm D} = 0.1503$	9	4.682	4.115
$C_{PM} = -0.4784$	10	6.136	5.505